

Adaptive Position Tracking Control of a BLDC Motor using a Recurrent Wavelet Neural Network

Chun-Fei Hsu¹ Chih-Min Lin^{2*} Chao-Ming Chung²

¹Department of Electrical Engineering, Chung Hua University, Hsinchu, 300, Taiwan, Republic of China

²Department of Electrical Engineering, Yuan Ze University, Chung-Li, Tao-Yuan, 320 Taiwan, Republic of China

Abstract: *The recurrent wavelet neural network (RWNN) has the advantages such as fast learning property, good generalization capability and information storing ability etc. Based on these advantages of RWNN, an adaptive position tracking control (APTC) system, which is composed of a neural controller and a robust controller, is proposed in this paper. The neural controller uses the RWNN structure to online mimic an ideal controller, and the robust controller is designed to achieve tracking performance with desired attenuation level. The adaptive laws of APTC system are derived based on the Lyapunov stability theorem and gradient decent method. Finally, the proposed APTC method is applied to a brushless DC (BLDC) motor. The hardware implementation of APTC scheme is developed on a field programmable gate array (FPGA) chip. Experimental results verify that a favorable tracking response can be achieved by the proposed APTC method even under the change of position command frequency after training of RWNN.*

Keywords: *Adaptive control, recurrent neural network, wavelet neural network, BLDC,*

1. INTRODUCTION

With the learning ability of neural network, neural networks have widely been recognized as a powerful tool in industrial control, commercial prediction, image processing applications and etc. (Mendel, 1994). The characteristics of fault tolerance, parallelism and learning suggest that they may be good candidates for implementing real-time adaptive control for unknown nonlinear dynamic systems (Omidvar and Elliott, 1997). The successful key element is the approximation ability of neural network, where the parameterized neural network can approximate an unknown system dynamics through some learning algorithms. Many authors have hinted the neural networks as powerful building blocks for a wide class of complex nonlinear system control strategies when there exists no complete model information or a controlled plant is considered as a "black box" (Hsu *et al.*, 2005; Leu *et al.*, 2005; Polycarpou, 1996; Tang *et al.*, 2006).

Recently, some researchers have developed the structure of neural network based on the wavelet functions to construct the wavelet neural network (WNN) (Billings and Wei, 2005; Zhang, 1997). Unlike the sigmoidal functions used in conventional neural networks, wavelet functions are spatially localized, so that the learning capability of WNN is more efficient than the conventional sigmoidal function neural network for system identification. The training algorithms for WNN typically converge in a smaller number of iterations than for the conventional neural networks (Zhang, 1997). Up to now, there has been considerable interest in exploring

the applications of WNN to deal with nonlinearity and uncertainties of real-time adaptive control system (Hsu *et al.*, 2006; Lin, 2002; Sousa *et al.*, 2002). These WNN-based adaptive neural controllers combine the capability of neural networks for learning ability and the capability of wavelet decomposition for identification ability.

Although the control performances are acceptable in (Hsu *et al.*, 2005; Hsu *et al.*, 2006; Leu *et al.*, 2005; Lin, 2002; Sousa *et al.*, 2002; Tang *et al.*, 2006), these neural networks are feedforward neural networks belonging to static mapping networks. Without aid of tapped delay, a feedforward neural network is unable to represent a dynamic mapping. In addition, the neural network must be selected with a sufficiently large number of neurons in the hidden layer, which consumes a large amount of processing time for real-time applications (Juang *et al.*, 2007; Lin and Lee, 1996). According to the structure, the recurrent neural network has superior capabilities as compared to feedforward neural networks, such as their dynamic response and their information storing ability. Since the recurrent neural network captures the dynamic response of a system, the network model can be simplified (Lin and Lee, 1996).

This paper proposes a recurrent wavelet neural network (RWNN), which has superior capability to the conventional WNN in an efficient learning mechanism and dynamic response. Temporal relations are embedded in RWNN by adding feedback connections, so that the RWNN provides a dynamical mapping. Then, an adaptive position tracking control (APTC) system using RWNN approach is proposed

to tackle the control problem of the brushless DC (BLDC) motor, which is ideal for use in expensive environments such as aeronautics, robotics, electric vehicles and dynamic actuation. All the parameters of the proposed APTC system are online tuned in the Lyapunov sense and gradient decent, thus the stability of the closed-loop system can be guaranteed. Finally, the proposed APTC system is implemented on a field programmable gate array (FPGA) chip for possible low-cost and high-performance industrial applications. The experimental results demonstrate that the proposed APTC scheme can achieve favorable position tracking control for the BLDC motor even under the change of position command frequency. Moreover, the better tracking performance can be achieved as a specified attenuation level is chosen smaller.

2. PROBLEM STATEMENT OF BLDC MOTOR

During two decade years, brushless DC (BLDC) motors have gained widespread use in electric drivers. BLDC motors are ideal for use in expensive environments such as aeronautics, robotics, electric vehicles and dynamic actuation (Dote and Kinoshita, 1990). Unfortunately, the BLDC motor is a nonlinear system whose internal parameter values will change slightly with different input command and environments. Using these BLDC motors in high-performance drivers require advance and robust control methods. The system equations of BLDC motor driver in a d - q model can be expressed as (Rubaai *et al.*, 2002; Rubaai *et al.*, 2007).

$$i_{qs} = -\frac{R_s}{L_q} i_{qs} - \frac{L_d}{L_q} \omega_r i_{ds} + \frac{1}{L_q} v_{qs} - \frac{\lambda_m}{L_q} \omega_r \quad (1)$$

$$i_{ds} = -\frac{R_s}{L_d} i_{ds} + \frac{L_q}{L_d} \omega_r i_{qs} + \frac{1}{L_d} v_{ds} \quad (2)$$

$$L_q = L_{is} + L_{mq} \quad (3)$$

$$L_d = L_{is} + L_{md} \quad (4)$$

where i_{ds} and i_{qs} represent the d and q axes stator currents, respectively, V_{ds} and V_{qs} are the d and q axes stator voltage, respectively, L_{ds} and L_{qs} are the d and q axes stator inductances, respectively, R_s is the stator resistance, L_{is} is the stator leakage inductance, L_{md} and L_{mq} are the d and q axes magnetizing inductances, respectively, ω_r is the electrical rotor angular velocity, and λ_m is the flux linkage of permanent magnet. The torque equation is expressed as (Rubaai *et al.*, 2007).

$$J \frac{2}{N} \dot{\omega}_r + B \frac{2}{N} \omega_r = T_e - T_L \quad (5)$$

where N is the number of poles, J is the inertia of the rotor, B is the damping coefficient, T_e is the electromagnetic torque and T_L is the load disturbance. By using the field-oriented control, the electromagnetic torque of BLDC motor driver can be expressed as (Slotine and Li, 1991).

$$T_e = \frac{3}{2} \frac{N}{2} \lambda_m i_{qs} = k_t i_{qs} \quad (6)$$

where $k_t = \frac{3}{2} \frac{N}{2} \lambda_m$ is the constant gain. From (5) and (6), the system dynamic equation can obtain

$$\ddot{\theta} = f \dot{\theta} + g u + h \quad (7)$$

where θ is a position of rotor, $f = -\frac{B}{J}$, $g = \frac{N}{2} \frac{k_t}{J}$,

$h = -\frac{N}{2J} T_L$, and $u = i_{qs}$ is the control effort. The control

objective of BLDC motor is to find a control law so that the rotor position θ can track the position command θ_c closely. Define the tracking error as

$$e = \theta_c - \theta \quad (8)$$

Assume that all the parameters in (7) are well known, there exists an ideal controller (Slotine and Li, 1991).

$$u^* = g^{-1} (-f \dot{\theta} - h + \ddot{\theta}_c + k_1 \dot{e} + k_2 e) \quad (9)$$

where k_1 and k_2 are non-zero positive constants. Applying the ideal controller (9) into (7), it is obtained that

$$\ddot{e} + k_1 \dot{e} + k_2 e = 0 \quad (10)$$

If k_1 and k_2 are chosen to correspond the coefficients of a Hurwitz polynomial, it implies that $\lim_{t \rightarrow \infty} e = 0$ for any starting initial conditions. Since the system dynamics and the load disturbance may be unknown or perturbed in practical applications, the ideal controller u^* in (9) can not be precisely obtained.

Much research has been done to apply various approaches in the control field of BLDC motor (Liu *et al.*, 2005; Rubaai *et al.*, 2002; Rubaai *et al.*, 2007). A PI controller is proposed based on the completely understanding of the model and through some time-consuming design procedures; however, their performances generally depend on the working point, thus the control parameters which want to ensure proper behavior in all operating conditions are difficult to design (Liu *et al.*, 2005). Rubaai *et al.* (2002) proposed an adaptive fuzzy controller. In order to ensure the system stability, a compensation controller will be designed to dispel the approximation error. However, the most frequently used of compensation controller is like a sliding-mode control, which requires the bound of the approximation error. To solve this chattering problem, a robust adaptive fuzzy-neural-network controller had been developed (Rubaai *et al.*, 2007). Though the robust tracking performance can be achieved, the used neural network is a feedforward neural network. It may be selected with a sufficiently large number of hidden neurons, in which the computation loading is heavy.

3. APTC DESIGN

3.1. Description of RWNN

As shown in Fig. 1, the RWNN, is comprised of an input layer, a mother wavelet layer, a product layer and an output layer, is adopted to implement the neural controller. The RWNN output can perform the mapping according to

$$y = \sum_{j=1}^M \alpha_j \Theta_j = \sum_{j=1}^M \alpha_j \prod_{i=1}^L \phi_{ij}(z_{ij}) \quad (11)$$

where the subscript ij indicates the i th input term of the j th wavelet, α_j is the connection weight between the product nodes and output node, and $z_{ij} = \sigma_{ij}(x_i + \phi_{ij}^p r_{ij} - m_{ij})$. The σ_{ij} , m_{ij} and r_{ij} are the dilation factor, translation factor and recurrent factor, respectively, and the memory term ϕ_{ij}^p is the self-recurrent term of a wavelet. In addition, the mother wavelets are chosen as

$$\phi_{ij}(z_{ij}) = (1 - \sigma^2 z_{ij}^2) \exp(-z_{ij}^2). \quad (12)$$

For ease of notation, (11) can be expressed in a compact vector form as

$$y(\mathbf{x}, \boldsymbol{\alpha}, \mathbf{m}, \mathbf{r}) = \boldsymbol{\alpha}^T \Theta(\mathbf{x}, \boldsymbol{\sigma}, \mathbf{m}, \mathbf{r}) \quad (13)$$

where $\mathbf{x} = [x_1 \ x_2 \ \dots \ x_L]^T$ is the input vector, $\boldsymbol{\alpha} = [\alpha_1 \ \alpha_2 \ \dots \ \alpha_M]^T$, $\Theta = [\Theta_1 \ \Theta_2 \ \dots \ \Theta_M]^T$, $\boldsymbol{\sigma} = [\sigma_{L1} \ \sigma_{L2} \ \dots \ \sigma_{L2} \ \dots \ \sigma_{1M} \ \dots \ \sigma_{LM}]^T$, $\mathbf{m} = [m_{11} \ \dots \ m_{L1} \ m_{12} \ \dots \ m_{L2} \ \dots \ m_{1M} \ \dots \ m_{LM}]^T$ and $\mathbf{r} = [r_{11} \ \dots \ r_{L1} \ \dots \ r_{12} \ \dots \ r_{L2} \ \dots \ r_{1M} \ \dots \ r_{LM}]^T$. The architecture of the RWNN

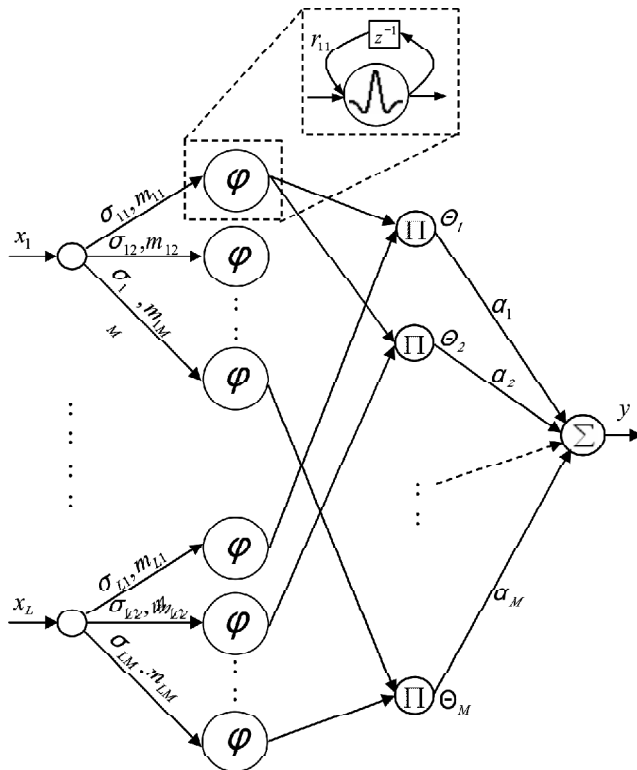


Figure 1: The Architecture of RWNN

used in this paper is designed to keep the advantage of simple structure and to consider the dynamic characteristics. The meaning of the recurrent network is to consider the past output of translation layer in the input space since the input of translation layer is related to its output. Thus, the RWNN has dynamic characteristics.

3.2. Design of APTC System

This study proposes an adaptive position tracking control (APTC) system as shown in Fig. 2, where the control law is designed as

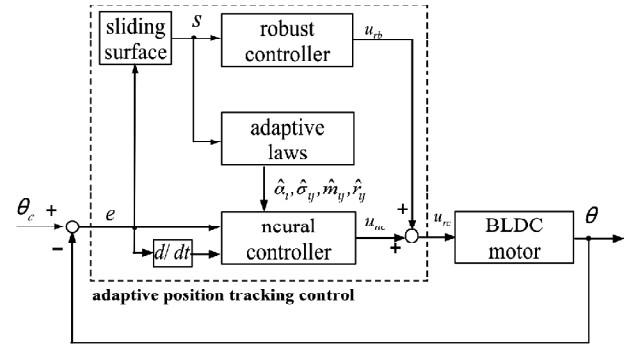


Figure 2: The Block Diagram of APTC System for BLDC Motor

$$u_{ac} = u_{nc} + u_{rb} \quad (14)$$

in which a sliding surface is defined as

$$s = \dot{e} + k_1 e + k_2 \int_0^t e(\tau) d\tau. \quad (15)$$

The neural controller u_{nc} uses a RWNN to online approximate the ideal controller in (9), and uses a robust controller u_{rb} is designed to achieve L_2 tracking performance with desired attenuation level. Substituting (14) into (7) and using (15), the error dynamic equation can be obtained as

$$\ddot{e} + k_1 \dot{e} + k_2 e = g(u^* - u_{nc} - u_{rb}) = \dot{s}. \quad (16)$$

According to the approximation theory, there exists an optimal RWNN approximator to approximate the ideal controller, which is denoted as (Billings and Wei, 2005).

$$u^* = \boldsymbol{\alpha}^{*T} \Theta + \Delta \quad (17)$$

where Δ denotes the approximation error and $\boldsymbol{\alpha}^*$ is the optimal parameter vector of $\boldsymbol{\alpha}$. In fact, the optimal parameter vector for neural network to approximate the ideal controller u^* is difficult to determine. To solve this difficulty, an estimative parameter vector is required to estimate the optimal value, and the neural network with estimative parameter vector is

$$u_{nc} = \hat{\boldsymbol{\alpha}}^T \Theta \quad (18)$$

where $\hat{\boldsymbol{\alpha}}$ is the estimative parameter vector of $\boldsymbol{\alpha}$. Then the estimative error between ideal controller and neural controller is defined as

$$\tilde{u} = u^* - u_{nc} = \boldsymbol{\alpha}^{*T} \Theta - \hat{\boldsymbol{\alpha}}^T \Theta + \Delta = \tilde{\boldsymbol{\alpha}}^T \Theta + \Delta \quad (19)$$

where $\tilde{\alpha} = \alpha^* - \hat{\alpha}$. Substitute equation (19) into equation (16) can obtain

$$\dot{s} = g(\tilde{\alpha}^T \Theta + \Delta - u_{rb}). \quad (20)$$

In case of the existence of Δ , consider a specified L_2 tracking performance (Lin and Lin, 2002; Wang *et al.*, 2002; Yang and Wang, 2007)

$$\int_0^T s^2 dt \leq \frac{s^2(0)}{g} + \frac{\tilde{\alpha}^T(0)\tilde{\alpha}(0)}{\eta_1} + \rho^2 \int_0^T \varepsilon^2 dt \quad (21)$$

where η_1 is a positive constant. If the system starts with initial conditions $s(0) = 0$ and $\tilde{\alpha}(0) = 0$, the L_2 tracking performance in (21) can be rewritten as

$$\sup_{\varepsilon \in L_2[0, T]} \frac{\|s\|}{\|\varepsilon\|} \leq \rho \quad (22)$$

where $\|s\|^2 = \int_0^T s^2 dt$ and $\|\varepsilon\|^2 = \int_0^T \varepsilon^2 dt$. The attenuation constant ρ can be specified by the designer to achieve desired attenuation ratio between $\|s\|$ and $\|\varepsilon\|$. If $\rho = \infty$, this is the case of minimum error tracking control without disturbance attenuation. To guarantee the stability of the APTC system, the Lyapunov function candidate is defined as

$$V = \frac{1}{2}s^2 + \frac{g}{2\eta_1}\tilde{\alpha}^T\tilde{\alpha}. \quad (23)$$

Taking the derivative of Lyapunov function in (23) and using (20), yields

$$\begin{aligned} \dot{V} &= s\dot{s} + \frac{g}{\eta_1}\tilde{\alpha}^T\dot{\tilde{\alpha}} \\ &= sg(\tilde{\alpha}^T\Theta + \Delta - u_{rb}) - \frac{g}{\eta_1}\tilde{\alpha}^T\dot{\tilde{\alpha}} \\ &= g\tilde{\alpha}^T\left(s\Theta - \frac{\dot{\tilde{\alpha}}}{\eta_1}\right) + sg(\varepsilon - u_{rb}). \end{aligned} \quad (24)$$

If the parameter tuning law is chosen as

$$\dot{\tilde{\alpha}} = \eta_1 s \Theta \quad (25)$$

and the robust controller is chosen as

$$u_{rb} = \frac{\rho^2 + 1}{2\rho^2}s \quad (26)$$

then (24) can be rewritten as

$$\begin{aligned} \dot{V} &= g\left[s\varepsilon - \left(\frac{\rho^2 + 1}{2\rho^2}\right)s^2\right] \\ &= g\left[-\frac{s^2}{2} - \frac{1}{2}\left(\frac{s}{\rho} - \rho\varepsilon\right)^2 + \frac{1}{2}\rho^2\varepsilon^2\right] \\ &\leq g\left[-\frac{s^2}{2} + \frac{1}{2}\rho^2\varepsilon^2\right]. \end{aligned} \quad (27)$$

Assume $\varepsilon \in L_2[0, T]$, $\forall T \in [0, \infty]$, integrating (27) from $t = 0$ to $t = T$, yields

$$V(T) - V(0) \leq -\frac{1}{2}g \int_0^T s^2 dt + \frac{1}{2}g\rho^2 \int_0^T \varepsilon^2 dt. \quad (28)$$

Since $V(T) \geq 0$, the above inequality implies the following inequality

$$\frac{1}{2}g \int_0^T s^2 dt \leq V(0) + \frac{1}{2}g\rho^2 \int_0^T \varepsilon^2 dt. \quad (29)$$

Using (23), (29) is equivalent to (21). Since $V(0)$ is finite, if the approximation error $\varepsilon \in L_2$, that is

$\int_0^T \varepsilon^2(t) dt < \infty$, using the Barbalat's lemma (Slotine and Li, 1991), the APTC system is stable with L_2 tracking performance in Lyapunov sense.

3.3. Full-tuned Online Learning Laws

Although the parameter tuning law in previous sub-section can modify the weights of output layer to the optimal values, the performance and converge speed are still affected by the parameter vectors in translation layer. If the variances, means and recurrent weights in translation layer are selected in appropriate value, the network will converge at high speed as well as high performance. However, the optimal values of parameter vectors in translation layer are not easy to find. In order to get the optimal parameter values of translation layer, the online tuning laws which are derived by Lyapunov function and gradient decent method are proposed to tune these parameters. To obtain the online tuning laws, first, the adaptive law in equation (25) can be rewritten as

$$\dot{\hat{\alpha}}_j = \eta_1 s \Theta_j \quad (30)$$

According to gradient decent method, this adaptive law can also be presented as

$$\dot{\hat{\alpha}}_j = -\eta_1 \frac{\partial V}{\partial u} \frac{\partial u}{\partial \hat{\alpha}_j} = -\eta_1 \frac{\partial V}{\partial u} \Theta_j \quad (31)$$

Comparing equation (31) with equation (30), the Jacobian term of the controlled system can be obtained as

$\frac{\partial V}{\partial u} = -s$. Therefore, the online tuning laws of variances, means and recurrent weights can be presented as

$$\begin{aligned} \dot{\hat{\sigma}}_{ij} &= -\eta_2 \frac{\partial V}{\partial u} \frac{\partial u}{\partial \hat{\sigma}_{ij}} = -\eta_2 \frac{\partial V}{\partial u} \frac{\partial u}{\partial \Theta_j} \frac{\partial \Theta}{\partial \hat{\sigma}_{ij}} \\ &= \eta_2 s \hat{\alpha}_j \Theta_j \left[\frac{-2w^2 \sigma_{ij} (x_i + r_{ij} \phi_{ij}^p - m_{ij})^2}{1 - w^2 \sigma_{ij}^2 (x_i + r_{ij} \phi_{ij}^p - m_{ij})^2} - 2\sigma_{ij} (x_i + r_{ij} \phi_{ij}^p - m_{ij})^2 \right] \end{aligned} \quad (32)$$

$$\dot{m}_{ij} = -\eta_3 \frac{\partial V}{\partial u} \frac{\partial u}{\partial m_{ij}} = -\eta_3 \frac{\partial V}{\partial u} \frac{\partial u}{\partial \Theta_j} \frac{\partial \Theta_j}{\partial m_{ij}}$$

$$\eta_3 s \hat{\alpha}_j \Theta_j \left[\frac{2w^2 \sigma_{ij}^2 (x_i + r_{ij} \phi_{ij}^p - m_{ij})}{1 - w^2 \sigma_{ij}^2 (x_i + r_{ij} \phi_{ij}^p - m_{ij})^2} + 2\sigma_{ij}^2 (x_i + r_{ij} \phi_{ij}^p - m_{ij}) \right] \quad (33)$$

$$\dot{r}_{ij} = -\eta_4 \frac{\partial V}{\partial u} \frac{\partial u}{\partial \hat{r}_{ij}} = -\eta_4 \frac{\partial V}{\partial u} \frac{\partial u}{\partial \Theta_j} \frac{\partial \Theta_j}{\partial \hat{r}_{ij}}$$

$$\eta_4 s \hat{\alpha}_j \Theta_j \left[\frac{-2w^2 \sigma_{ij}^2 \phi_{ij}^p (x_i + r_{ij} \phi_{ij}^p - m_{ij})}{1 - w^2 \sigma_{ij}^2 (x_i + r_{ij} \phi_{ij}^p - m_{ij})^2} - 2\sigma_{ij}^2 \phi_{ij}^p (x_i + r_{ij} \phi_{ij}^p - m_{ij}) \right] \quad (34)$$

Apply these online tuning laws into RWNN, the parameters in translation layer can be tuned to appropriate values. Therefore, the convergence can still be at high speed even if inappropriate initial parameters are given.

4. EXPERIMENTAL RESULTS

This study used the Altera Stratix II series FPGA chip, the Altera Quartus II software, the Nios II processor, the Nios II Integrated Development Environment (IDE) and the verilog hardware description language to implement the hardware control system. Field programmable gate array (FPGA) is a fast prototyping IC component. This kind of IC incorporates the architecture of a gate array and programmability of a programmable logic device. The advantage of controller implement by FPGA includes shorter development cycles, lower cost, small size, fast system execute speed, and high flexibility. The Quartus II software is the development tool for programmable logic devices. The Nios II processor is a configurable, versatile, RISC embedded processor. It can be embedded into Altera FPGA, and allow designers to integrate peripheral circuits and processors in the same chip. Additionally, the PC-developed algorithm and C language program can be rapidly migrated to the Nios II processor to shorten the system development cycle. The Nios II IDE can be accelerates software development (<http://www.altera.com>).

The external peripheral interfaces are used to transmit and receive the motor driver signals including motor rotational direction control signal circuit, encoder signal circuit, and 12-bits D/A converter circuit. The motor rotational direction control signal circuit uses the operational amplifier IC to raise the motor rotational direction control voltage up from the FPGA. The encoder signal circuit raises the encoder signal voltage up from the motor driver. The 12-bits D/A converter IC with dual channel voltage output is used to control the BLDC motor. Additionally, every IC that connects with the FPGA chip uses asynchronous bus transceiver IC to protect the current reflow to FPGA chip. The experimental setup is shown in Fig. 3. The proposed control algorithm is realized in the Nios II programming interface. The software flowchart of the control algorithm is shown in Fig. 4. In the main program, the initialization of controller parameters is preceded. Next, the interrupt interval

for the interrupt service routine (ISR) with a 1msec sampling rate is set. Then, the controller sample times can be governed by the built-in timer, which generates periodic interrupts.

The BLDC motor system offers high performance and simple operation from a compact driver and motor. The specifications of the adopted BLDC motor system manufactured by the Orientalmotor Company are outlined in Table I (<http://www.orientalmotor.com>). Modern mechanical systems often require high-speed high-accuracy linear motions. These linear motions are usually realized using the rotary motors with a mechanical transmission. The command using alternating sinusoidal and alternating stepped can supply the different linear motion speed. A second-order transfer function with 0.3 sec rise time of the following form is chosen as the reference model for the periodic step command

$$\frac{\omega_n^2}{\lambda^2 + 2\xi\omega_n\lambda + \omega_n^2} = \frac{400}{\lambda^2 + 40\lambda + 400} \quad (35)$$

where λ is the Laplace operator, ξ is damping ratio (set at one for critical damping) and ω_n is undamped natural frequency. The periodic step command can be specified in the reference model to smooth the reference trajectory. Moreover, in the proposed control system, without the second-order reference model the control input at the beginning will be very large due to the tracking error in the control algorithm. In addition, when the command is a sinusoidal reference trajectory, the trajectory of sinusoidal command doesn't need to change; therefore, the reference model is set as one.

First, an H^∞ adaptive fuzzy tracking control system proposed in Ref. (Rubaii *et al.*, 2007) is applied to BLDC motor. The experimental results of H^∞ adaptive fuzzy tracking control are shown in Fig. 5. The tracking responses are shown in Figs. 5(a) and 5(d), associated control efforts are shown in Figs. 5(b) and 5(e); and tracking errors are shown in Figs. 5(c) and 5(f), due to a sinusoidal command and a periodic step command, respectively. From the experimental results, though the H^∞ adaptive fuzzy tracking control can achieve tracking performances and there are no chattering phenomena in the control efforts; however, the convergence of the tracking error and controller parameters are very slow at beginning.

Then, the proposed APTC is applied to BLDC motor again. It should be emphasized that the development of APTC system does not need to know the system dynamics of the controlled system. For practical implementation, the parameters of the APTC system can be online tuned by the proposed adaptive laws without the need of system parameters. The control parameters for adaptive laws are chosen as $k_1 = k_2 = 4$, $\eta_1 = 0.02$ and $\eta_2 = \eta_3 = \eta_4 = 0.0002$. All the gains in the proposed control systems are chosen to achieve the best transient control performance in the considering the requirement of stability and possible

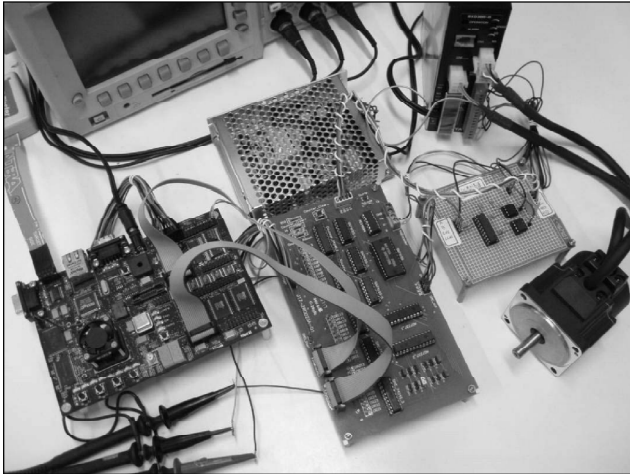


Figure 3: The Experimental Setup

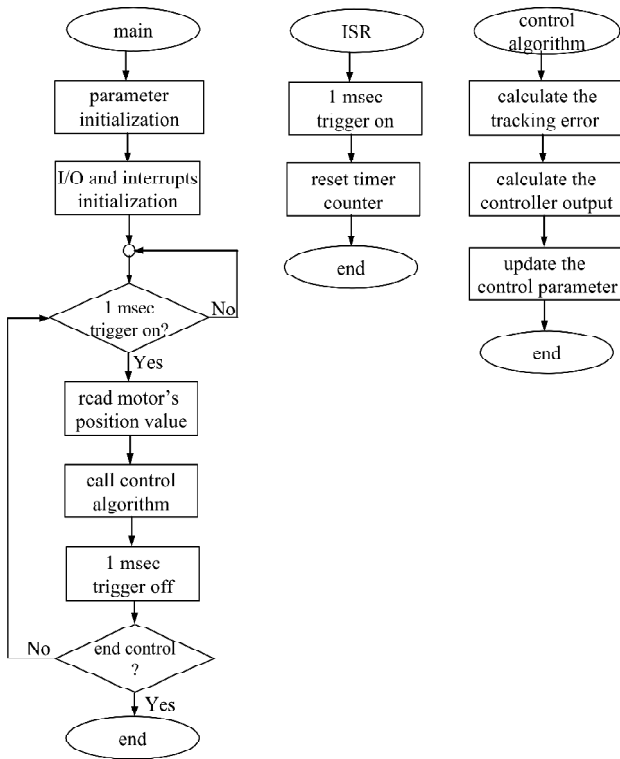


Figure 4: The Control Design Flow Chart

operating conditions. The experimental results of APTC with $\rho = 0.8$ are shown in Fig. 6. The tracking responses are shown in Figs. 6(a) and 6(d); associated control efforts are shown in Figs. 6(b) and 6(e); and tracking errors are shown in Figs. 6(c) and 6(f) due to a sinusoidal command and a periodic step command, respectively. If a specified attenuation level ρ is chosen smaller, the experimental results of APTC with $\rho = 0.5$ are shown in Fig. 7. The tracking responses are shown in Figs. 7(a) and 7(d); associated control efforts are shown in Figs. 7(b) and 7(e); and tracking errors are shown in Figs. 7(c) and 7(f) due to a sinusoidal command and a periodic step command, respectively. It is shown that the proposed

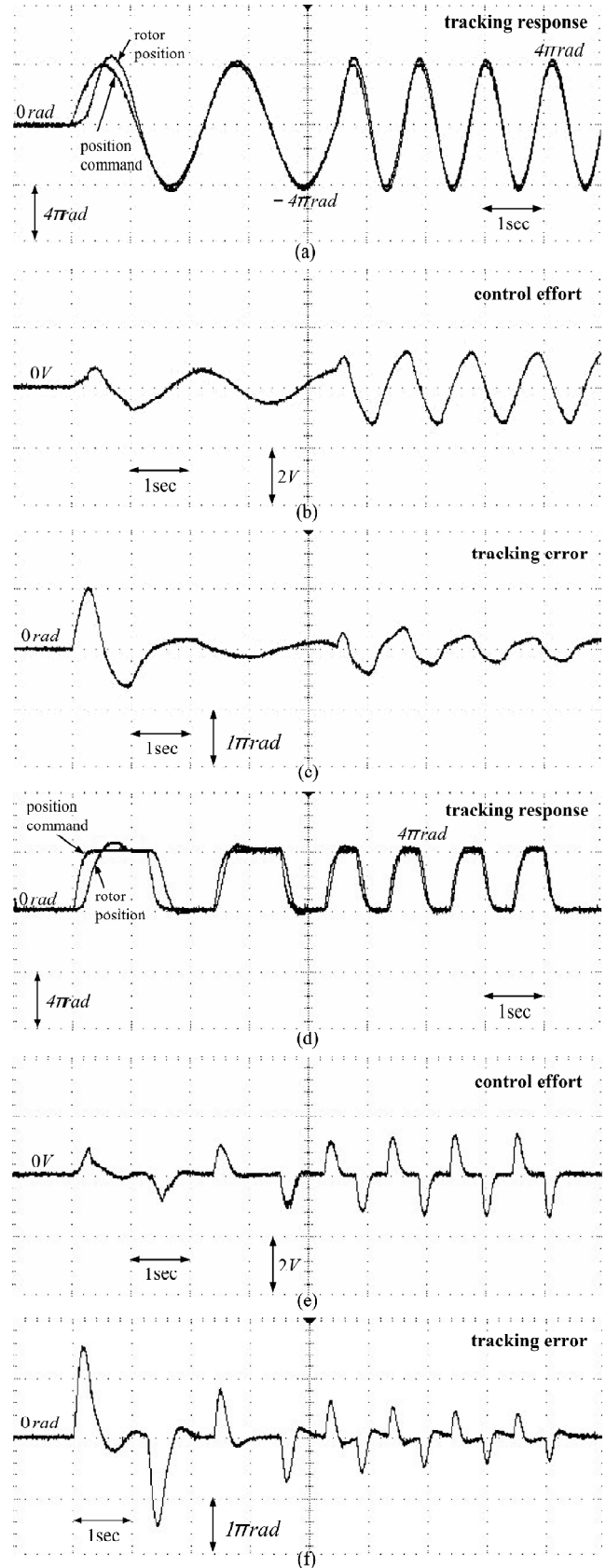


Figure 5: Experimental Results of H^∞ Adaptive Fuzzy Tracking Control

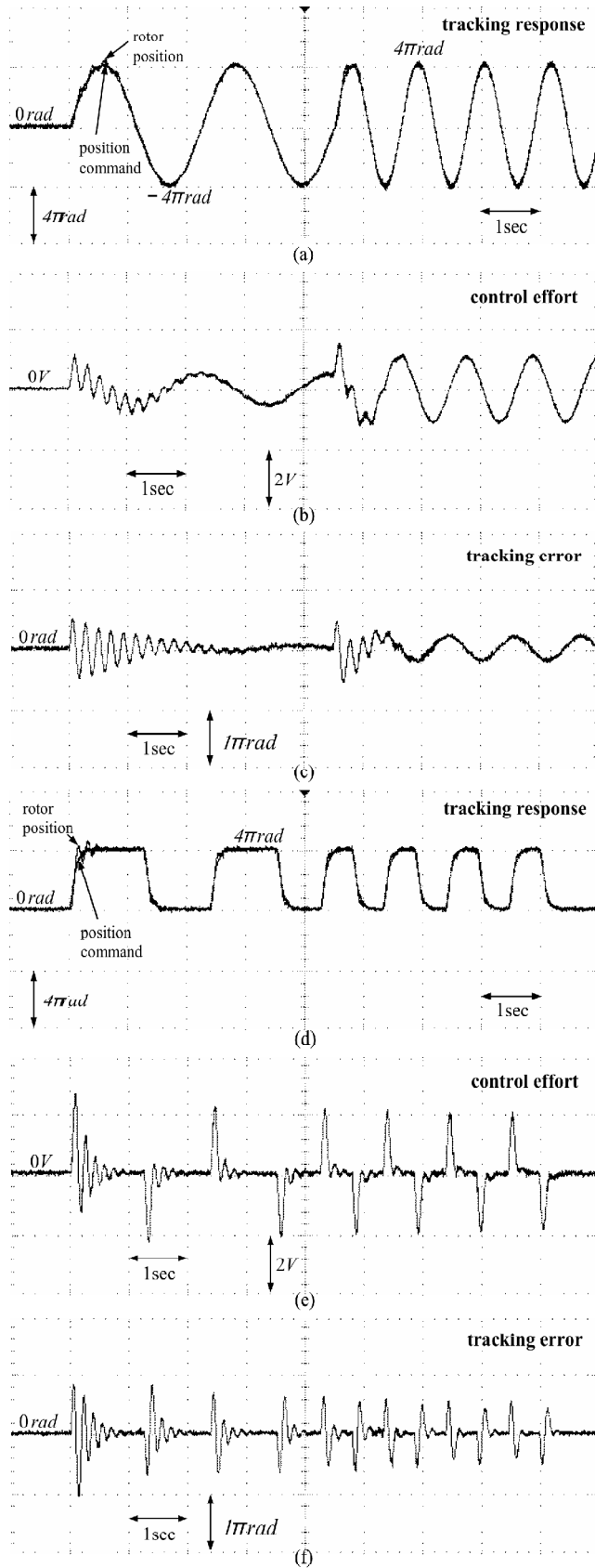


Figure 6: Experimental Results of APTC with $\rho = 0.8$

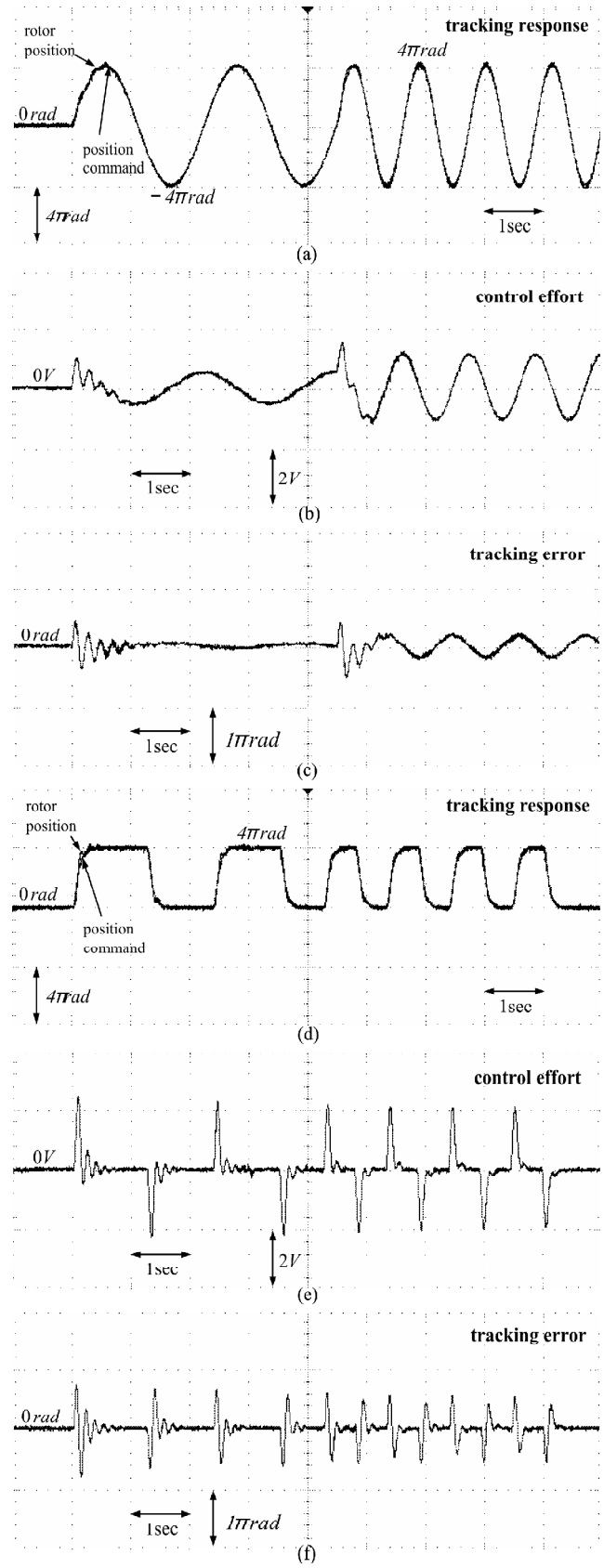


Figure 7: Experimental Results of APTC with $\rho = 0.5$

APTC can achieve favorable tracking performance; moreover, the better tracking performance can be achieved as a specified attenuation level ρ is chosen smaller.

Further, the trained APTC is applied to the BLDC system again. The experimental results of trained APTC with $\rho = 0.5$ are shown in Fig. 8. The tracking responses are shown in Figs. 8(a) and 8(d); associated control efforts are shown in Figs. 8(b) and 8(e); and tracking errors are shown in Figs. 8(c) and 8(f) due to a sinusoidal command and a periodic

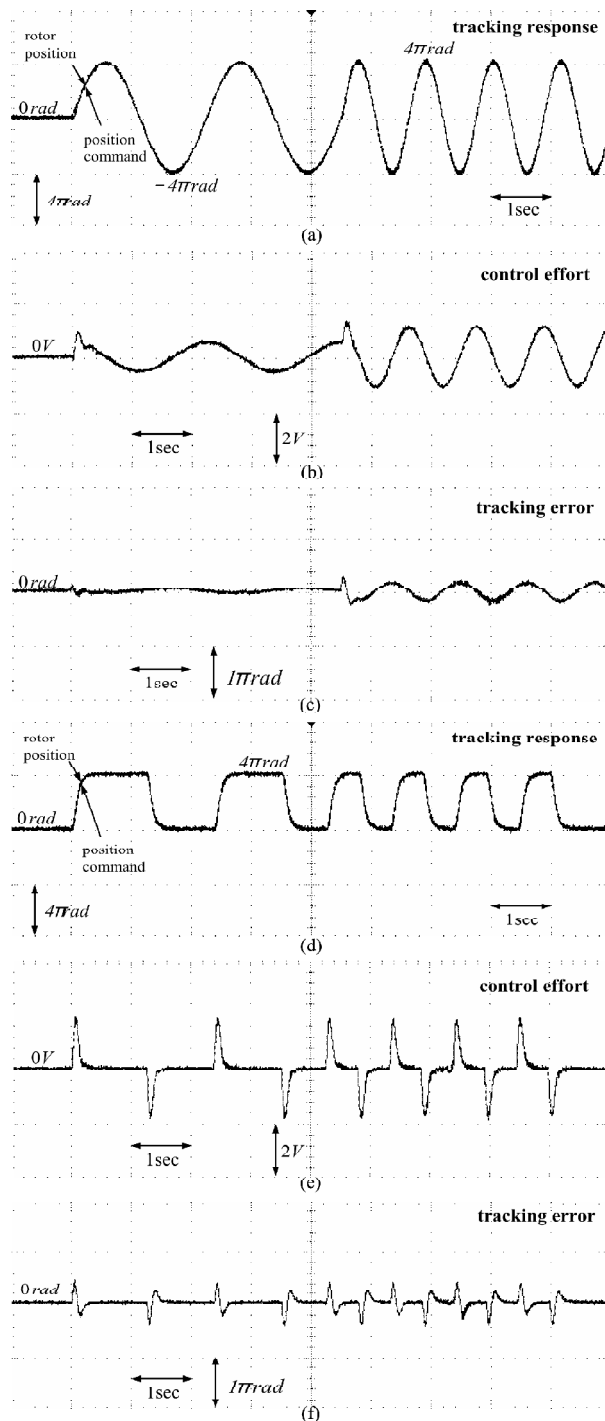


Figure 8: Experimental Results of Trained APTC with $\rho = 0.5$

Table I
The Specifications of BLDC Motor System

Output power HP (W)	1/25HP (30W)
Power supply	Single-phase 100~115VAC
Rated current	1.4 A
Gear/ shaft type	Round Shaft
Variable speed range	30 ~ 3000 r/min
Rated torque	0.1 N.m
Moment of inertia	$1.5 \cdot 10^{-4} \text{ kg} \cdot \text{m}^2$
Load of inertia	$0.088 \cdot 10^{-4} \text{ kg} \cdot \text{m}^2$
Components	BXD30A-A (Driver) BXM230-A2 (Motor)
Control detection system	Optimal encoder (500P/R)

step command, respectively. From the experimental results, it is seen that the tracking performance of the trained APTC is further improved when the initial values are trained, and they can achieve favorable robust characteristics for the command frequency variation.

5. CONCLUSIONS

This paper has successfully implemented an adaptive position tracking control (APTC) scheme for a brushless DC (BLDC) motor position tracking control on a field programmable gate array (FPGA) chip. Using the FPGA to implement, the APTC system can achieve the characteristics of small size, fast execution speed, less memory. Then, the effectiveness of the proposed APTC system is verified by some experimental results. The major contributions of this paper are: (1) the successful development of an APTC, in which the Lyapunov stability theorem and gradient decent is used to derive the online tuning algorithms. (2) the L_2 tracking performance can be achieved with a desired attenuation level using the proposed learning mechanism. (3) the successful applications of APTC to control a BLDC motor. And, the proposed APTC methodology can be easily extended to other motors. (4) the FPGA implementation consumes less power, in terms of core IC power consumption and especially in terms of the board-level power consumption, than the PC and DSP implementation.

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